

Determination of Rydberg's constant (R_H) to classify the structure of Hydrogen atom of Atomic Number (Z) = 1

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Abstract: The mass of a photon [1] is most important for creation of all types of particles and thus the universe. This article totally unknown to the scientists from the view of new idea. According to present presentation of physics, the characteristics and properties of particles setups which we call traditional process. Here we can adopt new idea to classify the Rydberg's constant to classifying the structure of Hydrogen atom which is more interesting and we will entire into unknown microscopic field. This field will explain particle's birth that in what way all these particles are interlinked beautifully. The field is very vast; here we will discuss this part only.

Keywords: Classification of atom, why electron and positron, gamma rays, ϕ and ϕ' photons, spectrum analysis, hydrogen structure.

I. Introduction

Up to about 40 years ago, it was thought that protons and neutrons were 'elementary' particles. But protons collided with other protons or electrons at high speed, indicated that they were made up of smaller particles. These particles were named 'quarks' by Murray Gell –Mann. There are a number of different varieties of quarks which are up, down, strange, charmed, bottom and top. Each has 3 colours—red, green and blue (this just for labels as quark has mass smaller, wavelength of visible light and do not have any colours in normal sense). Matter on the earth is made up mainly of protons and neutrons which are made up of quarks. There are no antiprotons and antineutrons, made up from antiquarks. In galaxy, there are no antiprotons and antineutrons apart from a smaller number that are produced as particles antiparticles pairs in high energy collisions, all galaxies are composed of quarks rather than antiquarks. The grand unified theory says that allows quarks to change into antielectrons at high speed or in reversed processes, antiquarks turning into electrons and electrons and antielectrons turning into antiquarks and quarks. In general, more quarks leads than antiquarks – the laws of physics do not require that assumption [2] because; for example,

$$e^+ + e^- = 2\gamma - \text{rays}$$

That is total energy of L.H.S. = total energy of R.H.S. will always be equal.

Classification of atom from the view of photonic eyes:

We have to think over the matter from the concept of photons that how we can define atom including subatomic particles for example,

Present concept: 1) An atom consists of main three particles electron (e^-), proton (p^+) neutron (n) and other subatomic particles with its antiparticles. In atom we see that there are three types of particles. Neutral particle has no charge, 2) Particles which has positive charge, 3) Particles which has negative charge.

1

New concept: If we consider all particles in two groups as:

1) e^- , p , n and subatomic particles like μ^+ , k^+ , π^+ , Σ^+ etc

2) e^+ and subatomic particles like μ^- , k^- , π^- , Σ^- etc in an atom and then we get the followings: Let, $\Delta_1 = \mu^+ + k^+ + \pi^+ + \Sigma^+$ etc (a)

$$\Delta_2 = \mu^- + k^- + \pi^- + \Sigma^- \text{ etc. (b)}$$

Then, $\Delta_1 / \Delta_2 = \Delta'$ (some definite quantity)

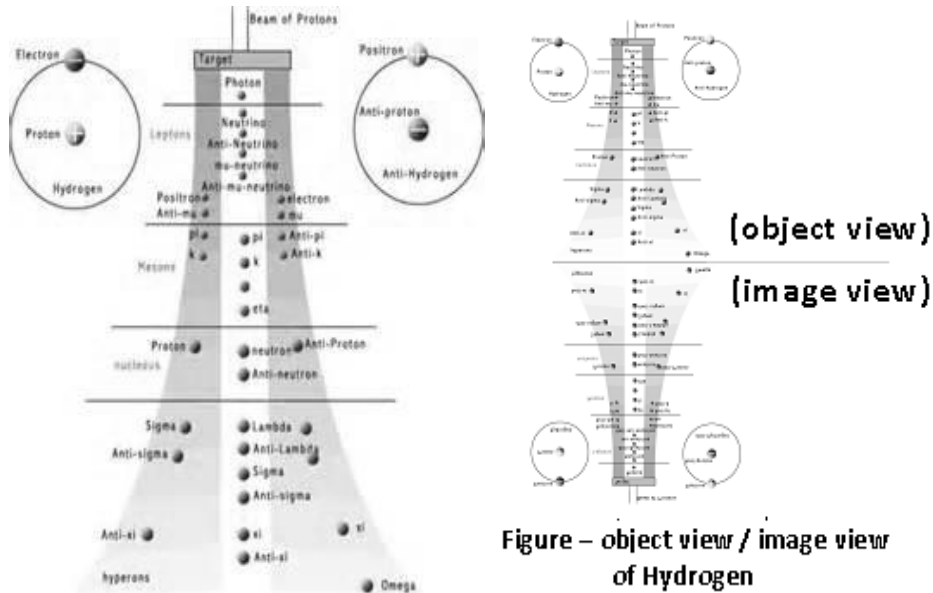
If Δ_1 is related with the particles e^- , p and n (object portion) and Δ_2 is related with a particle e^+ (image portion), then we can write,

$$\Sigma_{\text{atom}} = \frac{(e^- + p + n) \Delta_1}{e^+ \Delta_2} \dots \dots \dots \text{(c)}$$

$= \Phi \Delta' (e^+)^{-1}$, where, $(e^- + p + n) = \Phi \dots\dots\dots (d)$
 $= \Phi \Delta' e^-$ where, Σ_{atom} = ratio between the object and image of atom.

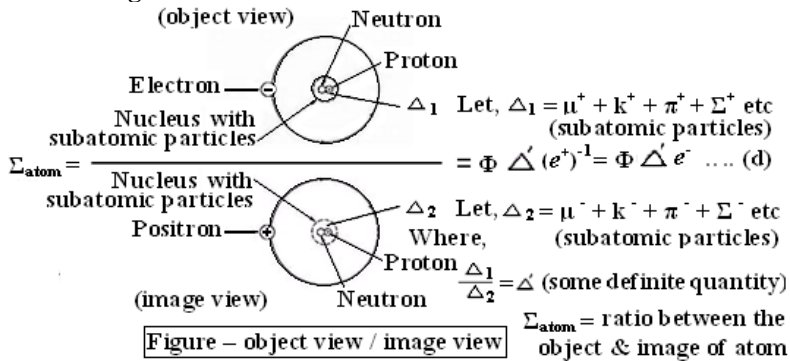
How positron may convert into an electron?

Suppose, we chose a number 10 and in reverse condition, 1/10 (=0.1). If 10 occupies in object portion and 1/10 in image portion, then, $10/0.1 = 10 \times 10 = 100$. Similarly, if electron (e^-) take position in object side and positron in image side, then, $e^- / e^+ = e^- \times e^- = e^{-2}$ may write. In the equation – (d), we have taken Φ as $(e^- + p + n)$ and then $\Phi \Delta'$ is expressing the combine particles electron, proton, neutron and subatomic particles. But $\Phi \Delta'$ with e^- as $\Phi \times \Delta' \times e^-$ is giving idea that total particles of an atom symbolized by Σ_{atom} . A figure of Hydrogen atom with subatomic particles is given here for an example [3].



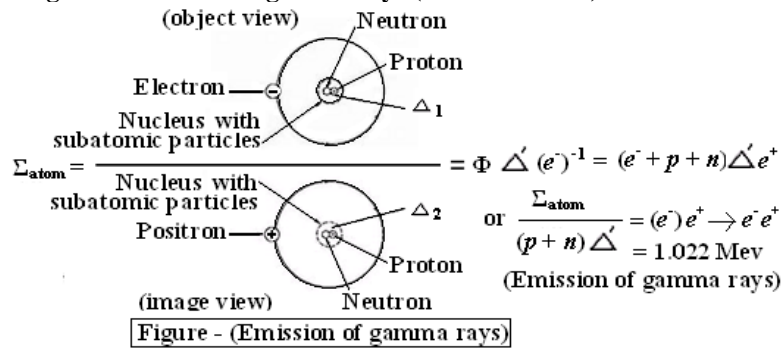
(Reference figure of Hydrogen with subatomic particles)

Therefore, we can draw a diagram of atom as:



This figure tells us that, the reverse form of electron is positron or vice versa. That means, when electron will move in clockwise direction, it will behave as an electron and this will liberate energy. And when electron will move in anticlockwise direction, it will behave as a particle, positron. In this position, when two electrons will move both the direction simultaneously (that is one in clockwise & other in anticlockwise direction), then it will emerge gamma (γ) rays.

Thus we can draw a figure of emission of gamma rays (A New Process):



We have the equation of mass of a photon [1] is

$$\sigma = \frac{2h^2}{N_A m_u \lambda_c^2 c^2} = 1.659619614 \times 10^{-54} \text{ gm} \dots \dots \dots \text{ (A)}$$

If we replace the mass of atom (m_u) in above equation by the mass of electron (m_e) then the mass of a photon will increase, which means we will get the mass of some bunch of photons. So, the mass of this populated photons may be devoted by σ_1 , then,

$$\sigma_1 = \frac{2h^2}{N_A m_e \lambda_c^2 c^2} = 3.025301565 \times 10^{-51} \text{ gm} \dots \dots \dots \text{ (B)}$$

Or $N_A \sigma_1 c^2 / [e] = 1.021998139 \text{ Mev (in terms of energy, } \gamma) \dots \dots \dots \text{ (C)}$

This is the energy of pair production of electron and positron ($e^- + e^+ = 1.022 \text{ Mev}$). The $\frac{1}{2}$ of the energy of the equation (C) is 0.510999 Mev or 0.511 Mev and this is the energy of electron. From the figure – gamma rays emission, we get, $e^- \times e^+ = 0.511 \text{ Mev} \times 0.511 \text{ Mev} = 0.26112 \text{ Mev}^2$, then, $\sqrt{0.26112 \text{ Mev}^2} = 0.511 \text{ Mev}$ which is the energy of an electron. So, energy of two particles in combine is $e^- + e^+ = 1.022 \text{ Mev}$. Again, from the view of the equation – C, the equation $N_A \sigma_1 c^2 / [e]$ is explaining that Avogadro's number (N_A) of populated photons (σ_1) in terms of energy ($c^2 / [e]$) is showing the energy of two electrons. Therefore, an electron is composed of $\frac{1}{2}$ of $N_A \sigma_1$ number of photons whatever the particle is electron or positron. In this formation of particles, we can tell that an atom is composed of electron, proton, neutron, subatomic particles with Avogadro number of photons which takes place in the atom in the form of energy.

Therefore, we can calculate the energy of particles and atomic weight of elements (known & unknown) by using the equation (d) in the following way:

If every particle within the atom is able to produce particular number of photons in excited state, then we will get some number of photons from that atom. If an electron, a proton, neutron is able to produce 1000, 10, 10 photons respectively, the we can write,

$$\begin{aligned} \Sigma_{\text{atom}} &= (e^- + p + n) \Delta' e^+, \\ &= (1000 + 10 + 10) \Delta' \times 1000 \\ &= (0.102 \times 10^4) \times 10^3 \Delta' = (\Phi') \times \Delta' \times 10^3 \text{ photons} \dots \dots \dots \text{ (e)} \end{aligned}$$

Here, $\Phi' = (0.102 \times 10^4)$ photons for an element Deuterium atom as it has one electron, one proton and one neutron.

If some amount of photons comes out from an element of atomic number Z and atomic weight m_0 , then we will get,

$$\begin{aligned} \Sigma_{m_0} &= N_A m_0 \Phi' \Delta' 10^3 / Z \text{ photons.} \dots \dots \dots \text{ (f)} \\ \text{For any element, } \Phi' &= Ze + Zp + (A - Z)n = Z10^3 + Z10 + (A - Z)10 \text{ photons... (g)} \end{aligned}$$

Where, $Z = e = p$ and $n = A - Z$

Again, we see that, $\Sigma_{m_0} = m_0 \times m_u / \sigma = m_0 / N_A \sigma$ photons $\dots \dots \dots \text{ (h)}$

From the equation (f) and (h) we get,

$$\Phi' \Delta' = 1 / N_A^2 \sigma 10^3 = 1.66146127 \times 10^3 \text{ photons.} = 1.54678376 \times 10^{-18} \text{ eV.} \dots \dots \dots \text{ (i)}$$

Knowing the value of $\Phi' \Delta' / Z$, we can determine the total number of photons of any element.

1. For an example,

Atomic weight of Hydrogen = $m_o = 1.0079$ atomic mass unit (amu) and then,
 $\Sigma_H = N_A \times 1.0079 \times 1.66146127 \times 10^{-27} \times 10^{-19} \text{ photons} = 1.008459071 \times 10^{30}$ photons. (Where, $N_A = 6.0221367 \times 10^{23}$ photons). Again, $\Sigma_H = \text{mass of Hydrogen} / \text{mass of a photon} = 1.0079 \text{ amu} / 1.659619614 \times 10^{-54} \text{ gm} = 1.008459071 \times 10^{30}$ photons. But, $1.66146127 \times 10^{-27} \times 10^{-19} / 2(3/2) = x \bar{\epsilon} = 6.31471826 \times 10^{-16} \text{ ev}$ which is almost equal to Planck constant as $\hbar/[e] = 6.582122 \times 10^{-16} \text{ ev-s}$, where, $j = 1 + 1/2$, $l = 1$, then, $j = 3/2 =$ angular quantum number and $\bar{\epsilon} = \text{energy of a photon} = 9.309779229 \times 10^{-22} \text{ ev}$. So, $\Phi' \Delta' / Z$ is important for microscopic field of particles.

2. We know that, $\Phi = 3.7 \times 10^{10} / 4\pi \times 10^4 = 2.944366447 \times 10^5$ photons [4]. ($\pi = 3.141592854$), We can get these photons from the following way:

$100 \times \sqrt{\pi} \times \Phi' \Delta' / Z = 2.944863426 \times 10^5$ photons. (j). Here the value of $\Phi' \approx \Phi$, varied after $1/1000^{\text{th}}$ decimal numbers. Therefore, the idea of Φ' for emission of photon from atom is justified. Knowing the value of Φ' from $\Phi' = Z_e + Z_p + (A - Z)n = Z10^3 + Z10 + (A - Z) 10$ photons, we can calculate the value of Δ' as,
 $\Delta' = Z / \Phi' \sigma N_A^2 \times 10^3 = 1.62 \dots$ Nearly constant for elements.

So, $\Delta' = \Delta_1 / \Delta_2 = 1.62 \dots$ Nearly constant, the ratio of subatomic particles as positive group / negative group. For higher atomic weight, $\Delta' = 1.6204 \dots$ the value of Δ' is different for each element, it differs only in decimal value (0.62) after 1.62 etc. But for lower atomic numbers for,

- 1) Hydrogen (mass = 1.0079 amu), $\Delta' = 1.645011158$
- 2) Helium (isotopic mass = 3.01605 amu), $\Delta' = 1.636907655$
- 3) Deuterium (mass = 2.0141 amu), $\Delta' = 1.628883598$.

Gradually this value of Δ' will decrease in decimal value when mass of element will increase. For example, mass of Radium = 226 amu, then, $\Delta' = 1.620039798$, from this verification, we may come to conclusion that $\Delta' = 1.6$ is constant for all elements. The values of Φ' photons are given in table photons for all known and unknown elements.

Determination of Rydberg's Constant ($R_H = 3.289841949 \times 10^{15} \text{ Hz}$).

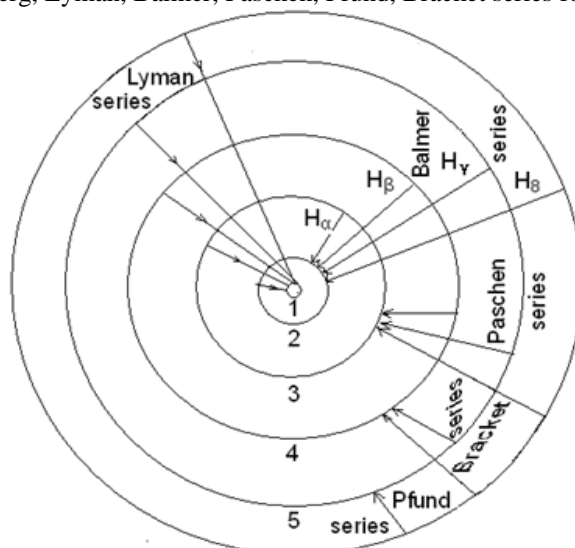
Bohr's theory of hydrogen spectrum gives the frequency of a special line as [5]:

$$\nu = \frac{2\pi^2 Z^2 m_e^4}{h^3} \times \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) = RZ^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) \dots\dots (1)$$

($R =$ Rydberg's Constant, $Z =$ Atomic Number, for Hydrogen = 1)

- i) Lyman series of special lines lying in the ultraviolet region, when, $n_1 = 1$ and $n_2 = 2, 3, 4$, etc.
- ii) Balmer series of visible region, when, $n_1 = 2$, $n_2 = 3, 4, 5$, etc.
- iii) Paschen series of infrared region, when, $n_1 = 3$, $n_2 = 4, 5, 6$, etc.

The relations between Rydberg, Lyman, Balmer, Paschen, Pfund, Bracket series for Hydrogen atom.



Transition of an electron in Bohr Model of Hydrogen atom.

So, Rydberg's constant (R_H) is most important that is interlinked to all series discovered by the scientists. Therefore, we need to find the value of R_H = 3.289841949x10¹⁵ Hz using Φ photons.

We already discussed about the Φ - photons and Φ' - photons. The three most stable isotopes of hydrogen: protium (A = 1), deuterium (A = 2), and tritium (A = 3). The Φ' values of these isotopes are: Φ'_P for Hydrogen or Protium = 0.101x10⁴ photons, Φ'_D for Deuterium = 0.102x10⁴ photons Φ'_T for Tritium = 0.103x10⁴ photons.

The value of Φ = 2.944366447x10⁵ photons, frequency of a photon $\bar{\nu} = 2.251093763 \times 10^{-7}$ Hz. And N_A = 6.0221367x10²³. Then the following arrangement gives the results as:

- i) 10 x {[N_A Φ'_P / Z Φ]} / √2} x $\bar{\nu} = 3.288203674 \times 10^{15}$ Hz, (Stable element)
- ii) 10 x {[N_A Φ'_D / Z Φ]} / √2} x $\bar{\nu} = 3.320760146 \times 10^{15}$ Hz, (Less stable element)
- iii) 10 x {[N_A Φ'_T / Z Φ]} / √2} x $\bar{\nu} = 3.353316618 \times 10^{15}$ Hz, (Least stable element)

Where, j = 1 + ½, l = 0 = quantum number.

The average value of Protium, Deuterium & Tritium is 3.320760146x10¹⁵ Hz. From these 3 results, we see that the frequency of Hydrogen **3.288203674x10¹⁵ Hz ≈ 3.289841949x10¹⁵ Hz**, the frequency of Rydberg's constant (R_H). Therefore, we can write the equation – 1 as,

$$\nu = \frac{10 \times N_A \Phi'}{\sqrt{2} Z \Phi} \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) \times \bar{\nu} \dots\dots\dots (2)$$

The value 10/√2 = 7.0710678 is almost to number 7, so the equation may write as,

$$\text{Or, } \nu = 7 \times \frac{N_A \Phi'}{Z \Phi} \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) \times \bar{\nu}$$

$$\text{Or, } \nu = \acute{n} \times \frac{N_A \Phi'}{Z \Phi} \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) \times \bar{\nu} \dots\dots\dots (3)$$

5 When, $\acute{n} = 1, 2, 3, 4, 5, 6, 7$ for lower frequency of Rydberg's frequency

When, $\acute{n} = 7$, then, $\nu = 3.2873848 \times 10^{15}$ Hz (13.59553 eV) ≈ 3.289841949x10¹⁵ Hz (13.60569 eV).

When, $\acute{n} = 6$, then, $\nu = 2.817758 \times 10^{15}$ Hz (11.6533 eV)

When, $\acute{n} = 5$, then, $\nu = 2.348132 \times 10^{15}$ Hz (9.71109 eV)

When, $\acute{n} = 4$, then, $\nu = 1.8785056 \times 10^{15}$ Hz (7.7688 eV)

When, $\acute{n} = 3$, then, $\nu = 1.4088792 \times 10^{15}$ Hz (5.8266 eV)

When, $\acute{n} = 2$, then, $\nu = 9.392528 \times 10^{14}$ Hz (3.88443 eV)

(upper range of visible spectrum, 7.69 – 6.59 x10¹⁴ Hz)

When, $\acute{n} = 1$, then, $\nu = 4.696264 \times 10^{14}$ Hz (1.94221 eV)

(Frequency of range of Red, 4.82 – 3.87 x10¹⁴ Hz).

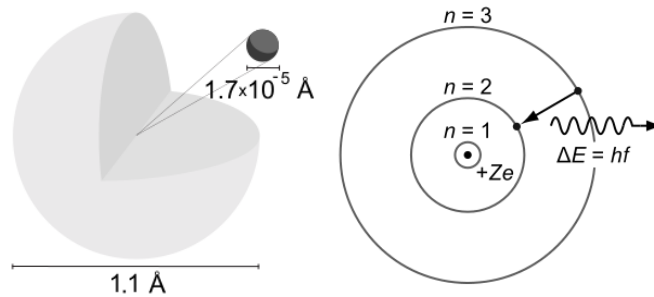
The frequency ranges of visible spectrum & energy range given here to compare the results.

Spectrum of visible range	Name of the Radiation	energy range (ñ within the range)
7.69 – 6.59 x10 ¹⁴ Hz	= Violet Radio frequency	0 – 10 ⁻⁵ eV
6.59 – 6.10 x10 ¹⁴ Hz	= Blue Microwave	10 ⁻⁵ – 10 ⁻³ eV
6.10 – 5.20 x10 ¹⁴ Hz	= Green Infrared	10 ⁻³ – 1.6 eV
5.20 – 5.03 x10 ¹⁴ Hz	= Yellow Visible	1.6 – 3.2 eV (1.94221 eV, ñ = 1)
5.03 – 4.82 x10 ¹⁴ Hz	= Orange Ultraviolet rays	3 – 2x10 ³ eV (ñ = 2, 3, 4..)
4.82 – 3.87 x10 ¹⁴ Hz	= Red X-ray	1.2x10 ³ – 2.4x10 ⁵ eV
	Gamma rays	10 ⁴ – 10 ⁷ eV

This is the advantage of the equation – 3 that we are not getting from the equation – 1. The number ñ may used to long numbers. When number will increase, we get different frequencies of the spectrum.

The perfect structure of Hydrogen has been drawn to use the equation – 3 and given here. By increasing number of ñ, we can get different types of energies of different particles. Traditionally the structure of hydrogen stated here in short:

In atomic physics, the Rutherford–Bohr model or **Bohr model**, introduced by Niels Bohr in 1913, depicts the atom as a small, positively charged nucleus surrounded by electrons that travel in circular orbits around the nucleus—similar in structure to the solar system.



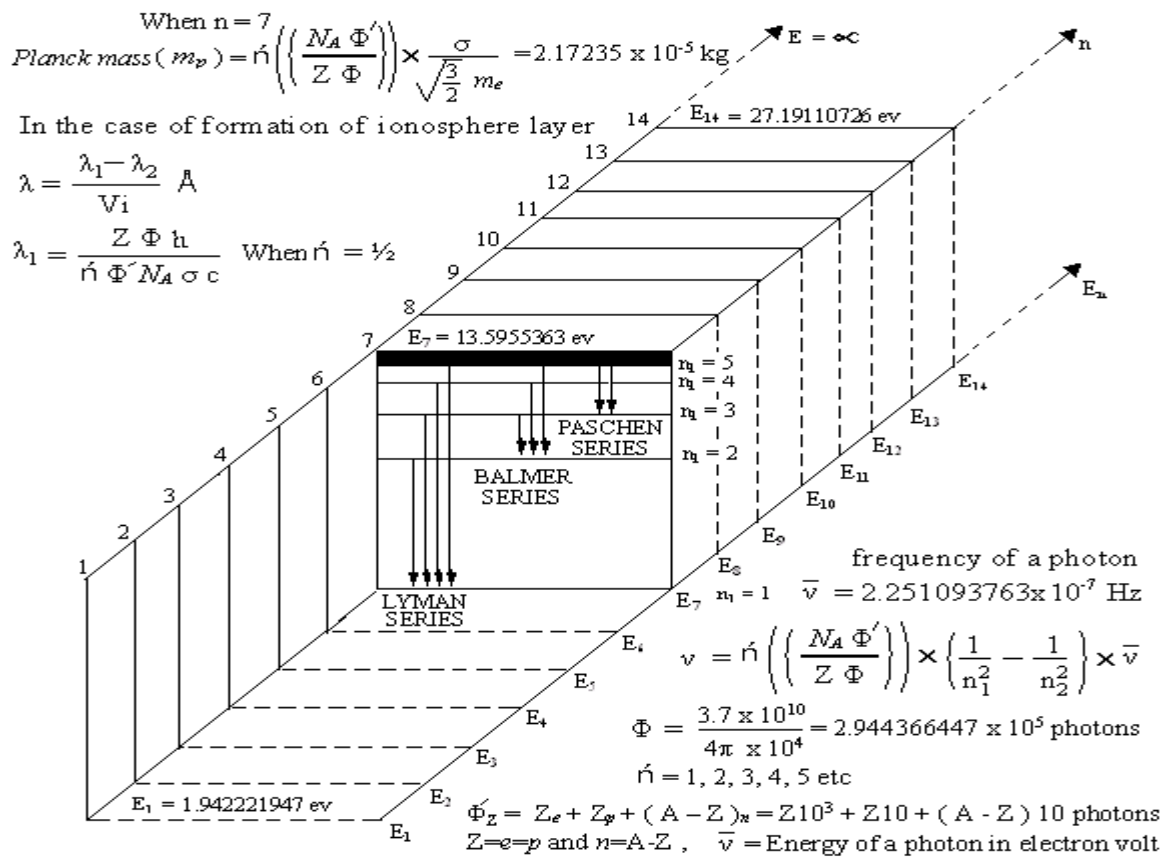
Depiction of a hydrogen atom showing the diameter as about twice the Bohr model radius. (Image not to scale, Fig - L. H. S.), Rutherford–Bohr model (Fig – R. H. S.).

6

The **Rutherford–Bohr model** of the hydrogen atom ($Z = 1$) or a hydrogen-like ion ($Z > 1$), where the negatively charged electron confined to an atomic shell encircles a small, positively charged atomic nucleus and where an electron jump between orbits is accompanied by an emitted or absorbed amount of electromagnetic energy ($h\nu$). The orbits in which the electron may travel are shown as grey circles; their radius increases as n^2 , where n is the principal quantum number. The $3 \rightarrow 2$ transition depicted here produces the first line of the Balmer Series and for hydrogen ($Z = 1$) it results in a photon of wavelength 656 nm (red light).

From the photonic idea, structure of the hydrogen gives more information on energy that how it interlinked to other states with quantum numbers. The descriptions are stated here through this diagram. The spectrum is not only a plane surface with length & height, when surface as like as very very thin paper, it must have breath also whatever the breath be negligible. We cannot ignore basically and omit the law of physics.

The information of various series in the HYDROGEN SPECTRUM



ENVIRONMENT OF LYMAN, BALMAR, PASCHEN

When, $\hbar = 7$, then we get 13.5955 eV for hydrogen, when, $\hbar = 14$, then, 27.19 eV to use the 7 equation, $\hbar \times \{ [(N_A \Phi'_H / Z \Phi)] / \sqrt{2} \} \times \bar{\nu}$ for hydrogen. On addition of Lyman series ($n_1 = 1$ and $n_2 = 2, 3, 4$, etc.), Balmer series ($n_1 = 2, n_2 = 3, 4, 5$, etc.), Paschen series ($n_1 = 3, n_2 = 4, 5, 6$, etc.) we reach to present results.

Determination of energy of Balmer series using equation - 156 for example:

For Balmer series, $n_1 = 2$ & $n_2 = 3$ to find the spectrum energy.

When, $(1/n_1^2 - 1/n_2^2) = (1/2^2 - 1/3^2) = 5/36 = 0.1388888$, then,

$v = 3.2873848 \times 10^{15} \text{ Hz} \times 0.1388888 = 4.56581219 \times 10^{14} \text{ Hz}$	$= 1.888 \text{ eV.}$	When, $n = 7.$
$v = 2.8177584 \times 10^{15} \text{ Hz} \times 0.1388888 = 3.913553308 \times 10^{14} \text{ Hz}$	$= 1.6185 \text{ eV.}$	When, $n = 6.$
$v = 2.348132 \times 10^{15} \text{ Hz} \times 0.1388888 = 3.261294124 \times 10^{14} \text{ Hz}$	$= 1.3487 \text{ eV.}$	When, $n = 5.$
$v = 1.8785056 \times 10^{15} \text{ Hz} \times 0.1388888 = 2.609035389 \times 10^{14} \text{ Hz}$	$= 1.0790 \text{ eV.}$	When, $n = 4.$
$v = 1.4088792 \times 10^{15} \text{ Hz} \times 0.1388888 = 1.956766541 \times 10^{14} \text{ Hz}$	$= 0.8092 \text{ eV.}$	When, $n = 3.$
$v = 9.392528 \times 10^{14} \text{ Hz} \times 0.1388888 = 1.304517694 \times 10^{14} \text{ Hz}$	$= 0.5395 \text{ eV.}$	When, $n = 2.$
$v = 4.696264 \times 10^{14} \text{ Hz} \times 0.1388888 = 6.522588847 \times 10^{13} \text{ Hz}$	$= 0.2697 \text{ eV.}$	When, $n = 1.$

For, Rydberg frequency, $3.289841949 \times 10^{15} \text{ Hz} \times 0.1388888 = 4.569224637 \times 10^{14} \text{ Hz}$ (1.889 eV).

The 1.889 eV almost equal to 1.888 eV obtained from the equation - 3, when, $n = 7$ and the **equation - 3 is producing more 6 result which we can't get from the equation - 1.**

Similarly, we can get other results when $[1/n_1]^2 - [1/n_2]^2 = [1/2]^2 - [1/4]^2 = 12/64 = 0.1875$ to follow the Balmer's series. Accordingly, we get,

(i) 2.5491 eV, when, $n = 7$, (ii) 2.1849 eV, when, $n = 6$, (iii) 1.8208 eV, when, $n = 5$, (iv) 1.4566 eV, when, $n = 4$, (v) 1.0924 eV, when, $n = 3$, (vi) 0.7283 eV, when, $n = 2$, (vii) 0.3641 eV, when, $n = 1$. It is observed that when n increases in Balmer series, then energy increases with respect to n . The equation - 3 is applicable to Lyman, Paschen, Pfund, Bracket series also.

This advantage certainly be developed the spectrum analysis in the microscopic fields. Therefore, Φ - photons and Φ' - photons is very useful to find many unknown phenomena in particle physics.

II. Conclusion

This is very simple classification to get answer of many particles that how actually particles created? The structure of Hydrogen atom through photonic mechanism is proving that all matter is composed of photons. We know lot of things on particles though needs to enter into it for searching other microscopic mechanisms which we are in dark. Also it is possible to find the atomic mass of all elements from 1 to 118 and unknown element after this number 118 by using Φ' - photons to follow the equation (g) as $\Phi' = Ze + Zp + (A - Z)n = Z10^3 + Z10 + (A - Z)10$ photons. All these are listed in my book "Endless Theory of the Universe (Complete Unified Theory)", Published by Lap Lambert, Germany, August, 2014.

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